

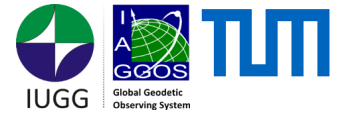
Strategy for the establishment of the International Height Reference System (IHRIS)

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Symposium SIRGAS2018
Aguascalientes, Mexico, Oct. 11, 2018

Outline



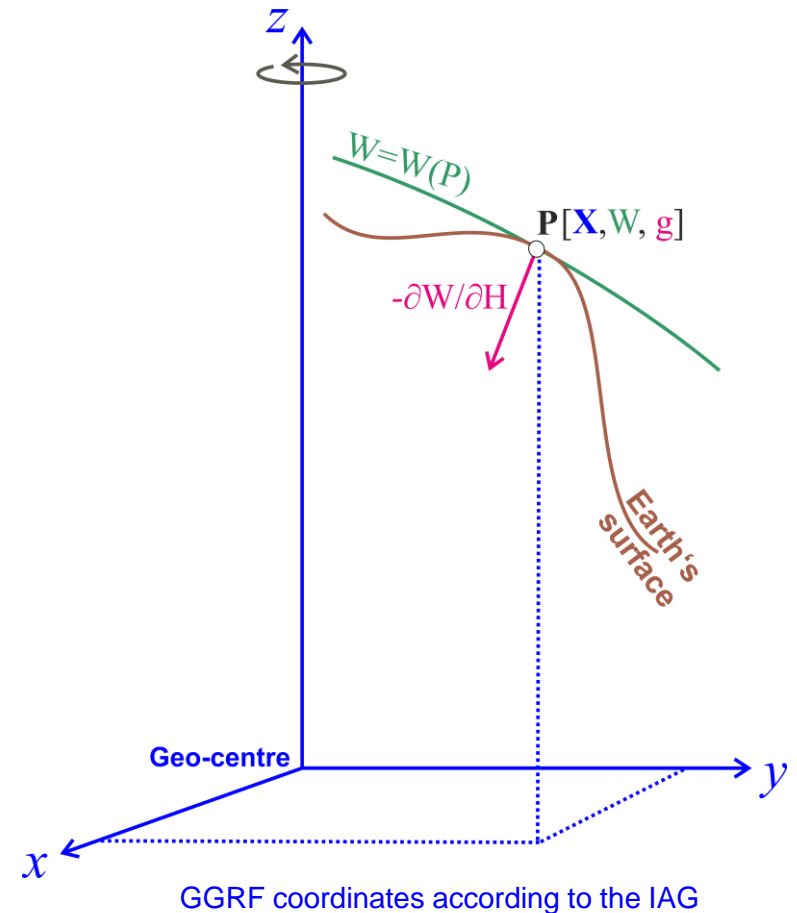
- 1) Motivation
- 2) The International Height Reference System (IHR)
- 3) The International Height Reference Frame (IHRF):
 - a) Physical realization: solid materialization by means of reference stations
 - Criteria for the station selection
 - Preliminary reference network for the IHRF
 - b) Mathematical realization: determination of reference coordinates in agreement with the definition of the IHR (preliminary computation of vertical coordinates)
- 4) Next steps

Motivation

A main objective of the [International Association of Geodesy \(IAG\)](#) and its [Global Geodetic Observing System \(GGOS\)](#) is the implementation of an integrated [Global Geodetic Reference Frame \(GGRF\)](#) that supports the consistent determination and monitoring of the Earth's geometry, rotation and gravity field with high accuracy worldwide.

The GGRF includes:

- Geocentric Cartesian coordinates $\mathbf{X}, \dot{\mathbf{X}}$
- Gravity vector $\mathbf{g}, \dot{\mathbf{g}}$
- Potential of the Earth's gravity field W, \dot{W}
- Physical height H, \dot{H}

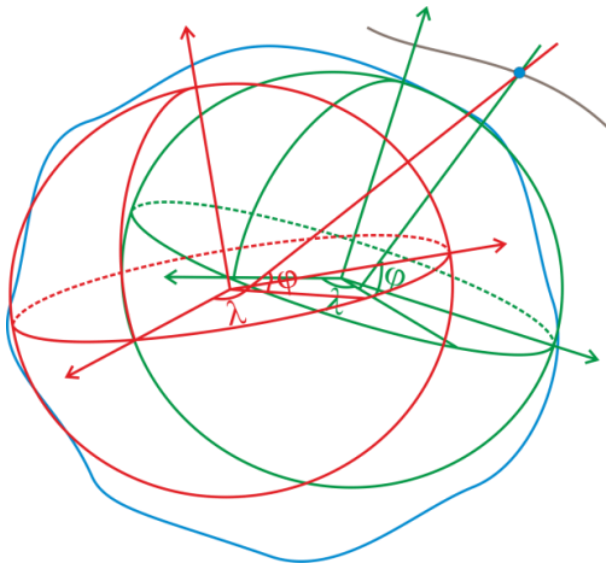


See: *Description of the Global Geodetic Reference Frame*; position paper adopted by the IAG Executive Committee, April, 2016, http://iag.dgfi.tum.de/fileadmin/IAG-docs/GGRF_description_by_the_IAG_V2.pdf

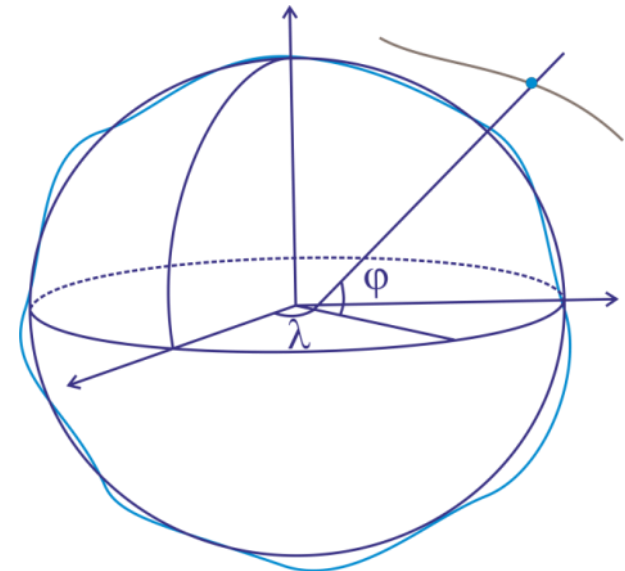
Geocentric Cartesian coordinates

refer to the International Terrestrial Reference System (ITRS) and Frame (ITRF)

- Standardized computation through the IERS (International Earth Rotation and Reference Systems' Service);
- Worldwide unified reference frame;
- Reliability at the cm-level.



Before the ITRS/ITRF: many individual (local) horizontal reference systems



Today: one global unified geocentric reference system

References for physical coordinates

1) Gravity observations refer to the International Gravity Standardization Net 1971 (IGSN71)

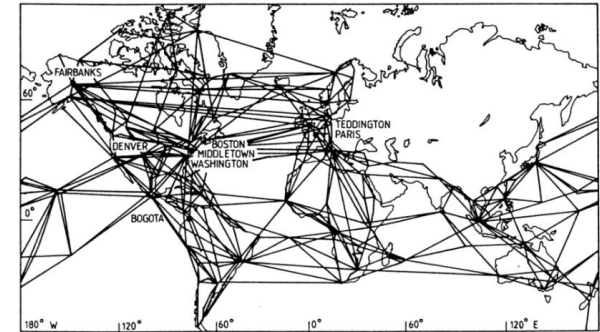
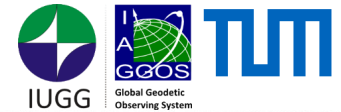
- Accuracy: $1\mu\text{ms}^{-2}$ ($100\ \mu\text{Gal}$)
- 10 absolute gravity stations
- 1,200 pendulum and 24,000 relative observations
- Potsdam datum correction -14mGal

2) Physical heights refer to more than 100 vertical datums

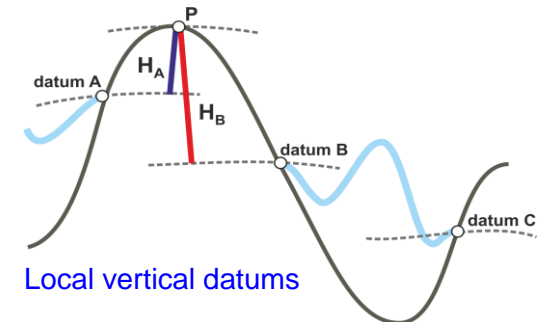
- Different reference levels (many [dm] of discrepancy);
- Different types of heights (normal, orthometric, etc.);
- Omission of (sea and land) vertical variations with time;
- Unprecise combination of h-H-N

3) (Static) geoid

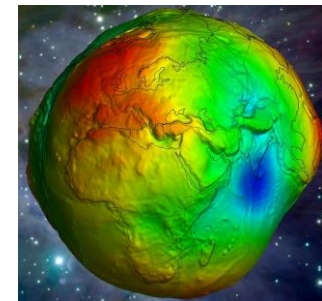
- Accuracy at the cm-level at the long wavelengths ($\sim 100\ \text{km}$) thanks to the satellite gravity missions, but more than 150 models since 2008
- Accuracy at the short wavelengths depends on the availability of terrestrial (airborne, marine) gravity data and terrain models
- Different geoid modelling approaches lead to different results (discrepancies of some dm).



IGSN71 (after Morelli et al. 1976)



Local vertical datums



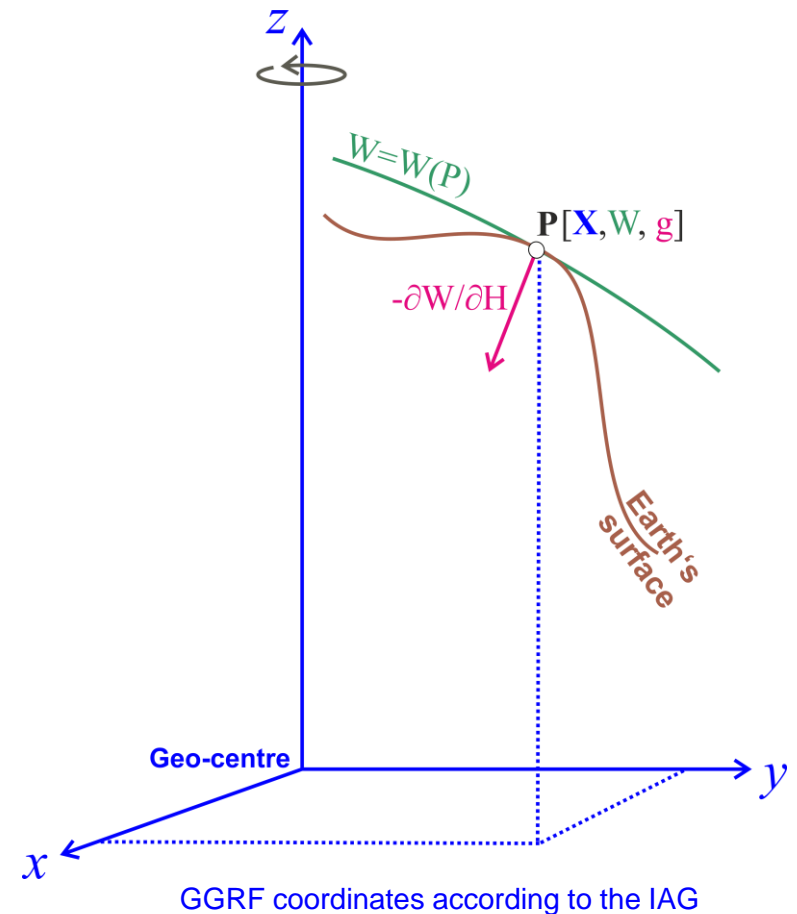
EIGEN-6C4 geoid model, ICGEM

IAG Resolutions 2015

The establishment of an integrated GGRF demands the implementation of a **worldwide-unified (standardized) physical reference system** able to support the high precision provided by the current geodetic observation techniques.

A first concrete step oriented to this purpose was the release of two IAG resolutions during the IUGG2015 General Assembly (Prague, July 2015):

- one for the **definition and realization of an International Height Reference System (IHR)**, and
- the second one for the **establishment of an International Gravity Reference System (IGRS)** based on absolute gravity measurements (as replacement of the IGSN71).



See: Drewes et al.: *The Geodesist's Handbook 2016*, Journal of Geodesy. 2016.

International Height Reference System (IHR)

IAG Resolution No. 1, Prague, July 2015

- 1) Vertical coordinates are **potential differences** with respect to a **conventionally fixed W_0** value:

$$C_P = C(P) = W_0 - W(P) = -\Delta W(P)$$

$$W_0 = \text{const.} = 62\,636\,853.4 \text{ m}^2\text{s}^{-2}$$

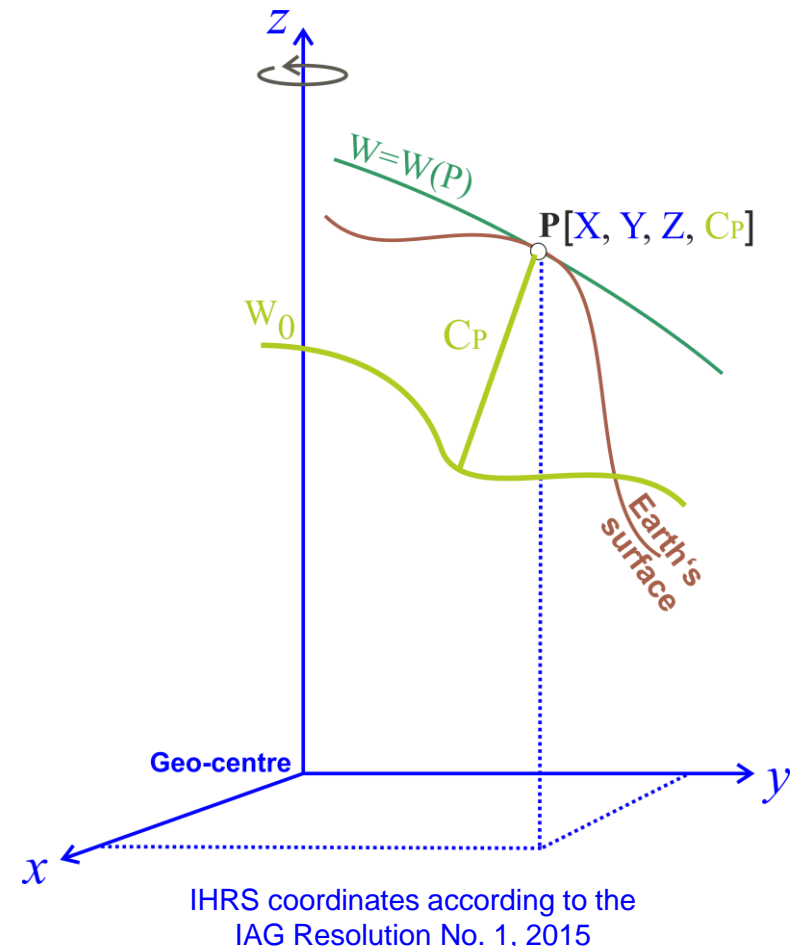
- 2) The position P is given in the ITRF

$$\mathbf{X}_P (X_P, Y_P, Z_P); \text{ i.e., } W(P) = W(\mathbf{X}_P)$$

- 3) The estimation of $\mathbf{X}(P)$, $W(P)$ (or $C(P)$) includes their variation with time; i.e., $\dot{\mathbf{X}}(P)$, $\dot{W}(P)$ (or $\dot{C}(P)$).

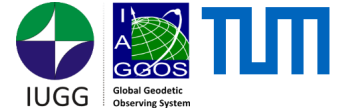
- 4) Coordinates are given in **mean-tide system / mean (zero) crust**.

- 5) The unit of length is the **meter** and the unit of time is the **second** (SI).



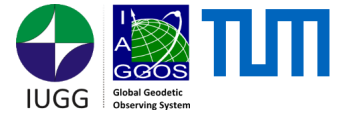
See: Ihde J. et al.: *Definition and proposed realization of the International Height Reference System (IHR)*. *Surv Geophy* 38(3), 549-570, 10.1007/s10712-017-9409-3, 2017

Primary actions to implement the IHRF and its realization IHRF



- 1) **Station selection** for the IHRF reference network
- 2) Strategy for the determination of **high-precise primary coordinates** \mathbf{X}_P , $\dot{\mathbf{X}}_P$, W_P , \dot{W}_P at the IHRF reference stations
- 3) Identification and preparation of **standards and conventions** to ensure consistency between the definition (IHRF) and the realization (IHRF); i.e., an equivalent documentation to the IERS conventions is needed for the IHRF/IHRF.

Activities related to the IHRF reference network



- 1) **Sep. 2016** (GGHS2016, Thessaloniki): Criteria for the selection of IHRF stations
- 2) **Oct. 2016** (GGOS Days 2016, Cambridge, MA): Preliminary IHRF station selection
- 3) **Nov. 2016 – Mar. 2017**: Interaction with regional and national experts about the preliminary station selection and proposal for further geodetic sites
- 4) **Apr. 2017** (EGU2017, Vienna): First proposal for the IHRF reference network
- 5) **At present**: refinement of the station selection with contributions from Japan, Africa and the IAG JWG 2.1.1 (Establishment of a global absolute gravity reference system). During the Gravity Symposium GGHS2018 (Copenhagen, Sep 17-21, 2018) initial contact with Israel, Nepal and Saudi Arabia to identify potential IHRF stations in those countries.

Criteria for the IHRF reference network configuration



1) Hierarchy:

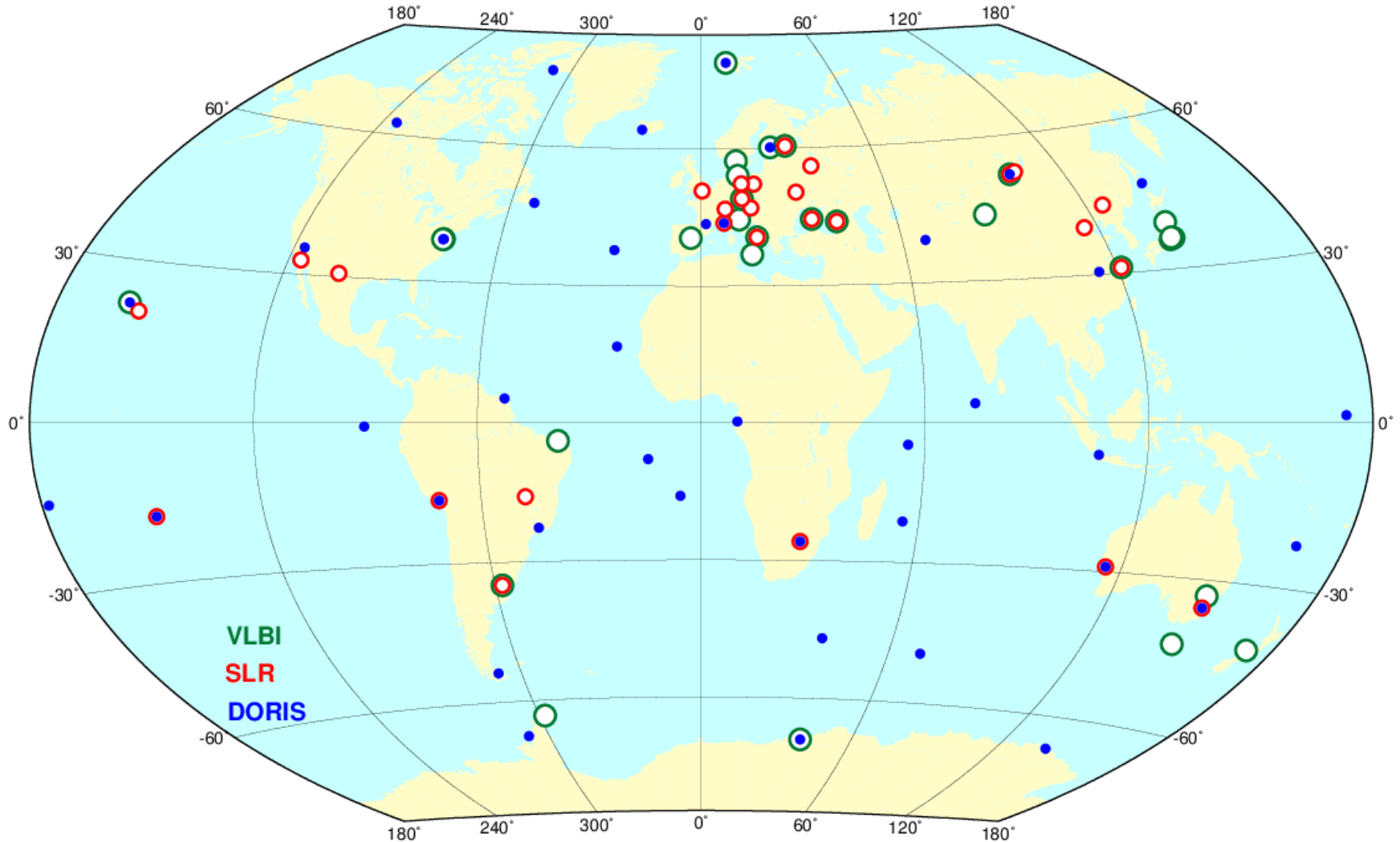
- A **global network** → worldwide distribution, including
- A **core network** → to ensure sustainability and long term stability
- **Regional and national densifications** → local accessibility

2) Collocated with:

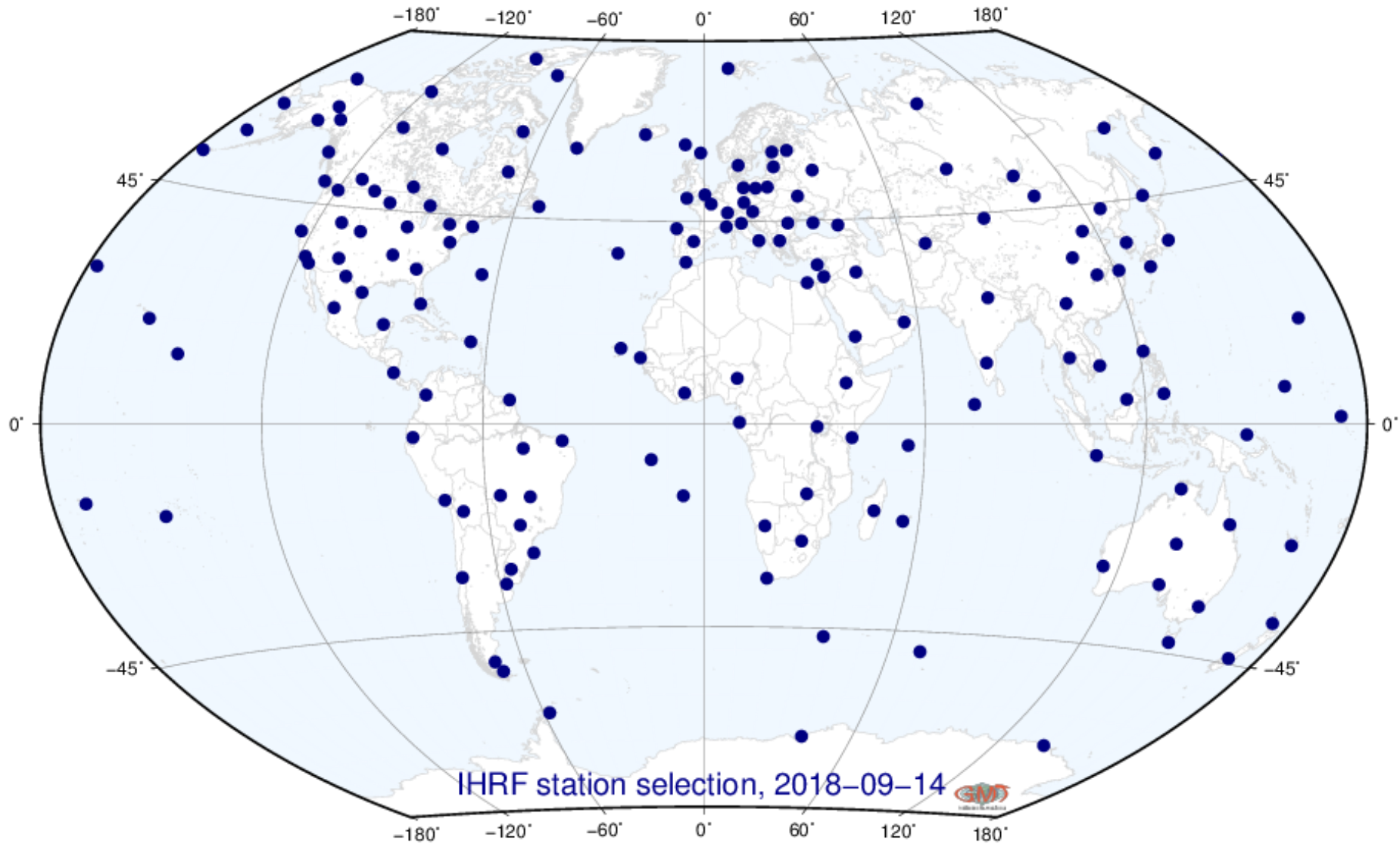
- fundamental **geodetic observatories** → connection between \mathbf{X} , W , \mathbf{g} and time realization (reference clocks) → **to support the GGRF**;
- **continuously operating reference stations** → to detect deformations of the reference frame (preference for ITRF and regional reference stations, like SIRGAS, EPN, APREF, etc.);
- **reference tide gauges and national vertical networks** → vertical datum unification;
- reference stations of the new **International Gravity Reference System** (see IAG Resolution 2, Prague 2015).

3) Main requirement: **availability of terrestrial gravity data around the IHRS reference stations for high-resolution gravity field modelling (i.e., precise estimation of W).**

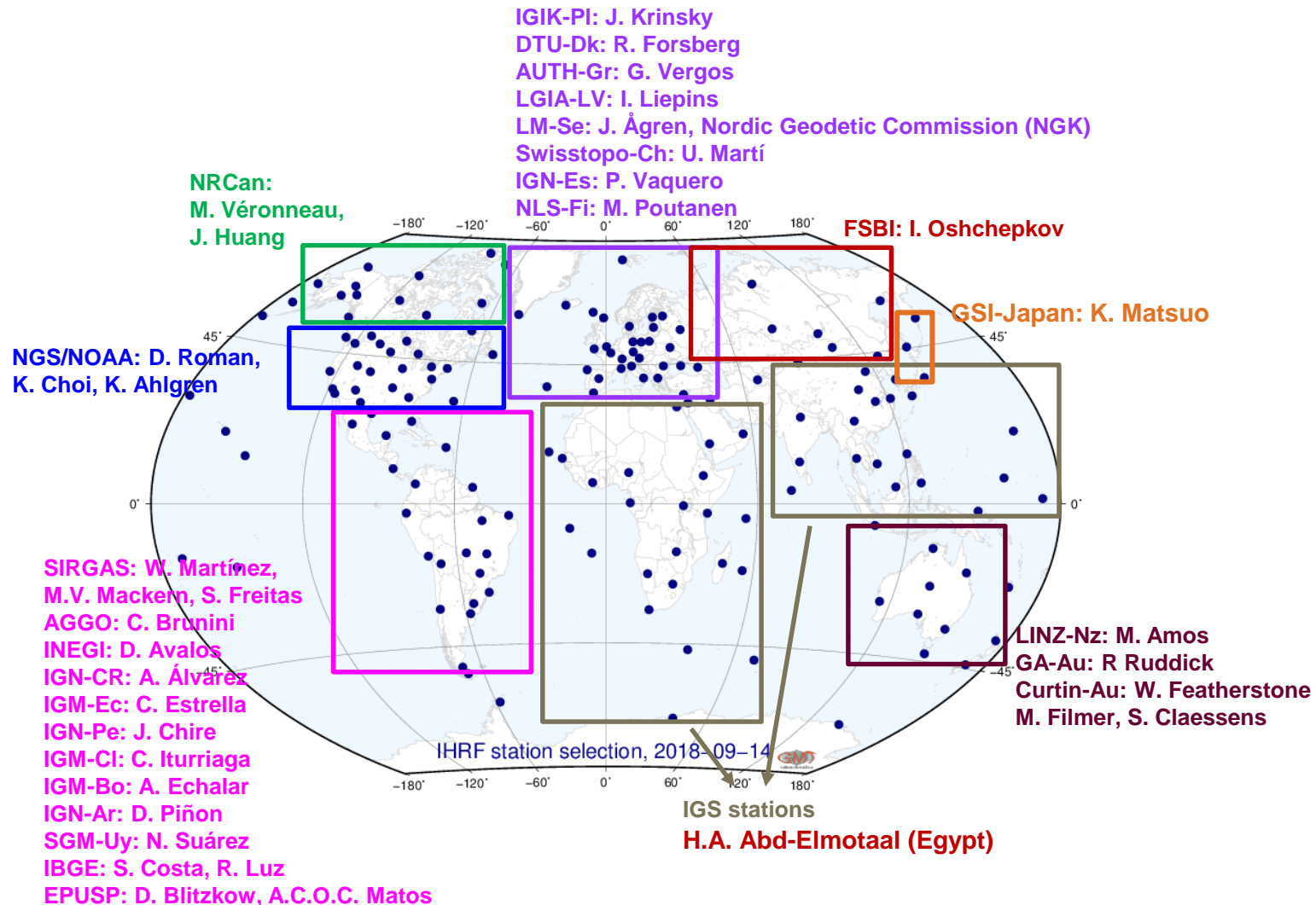
Preliminary station selection for the IHRF (Oct. 2016)



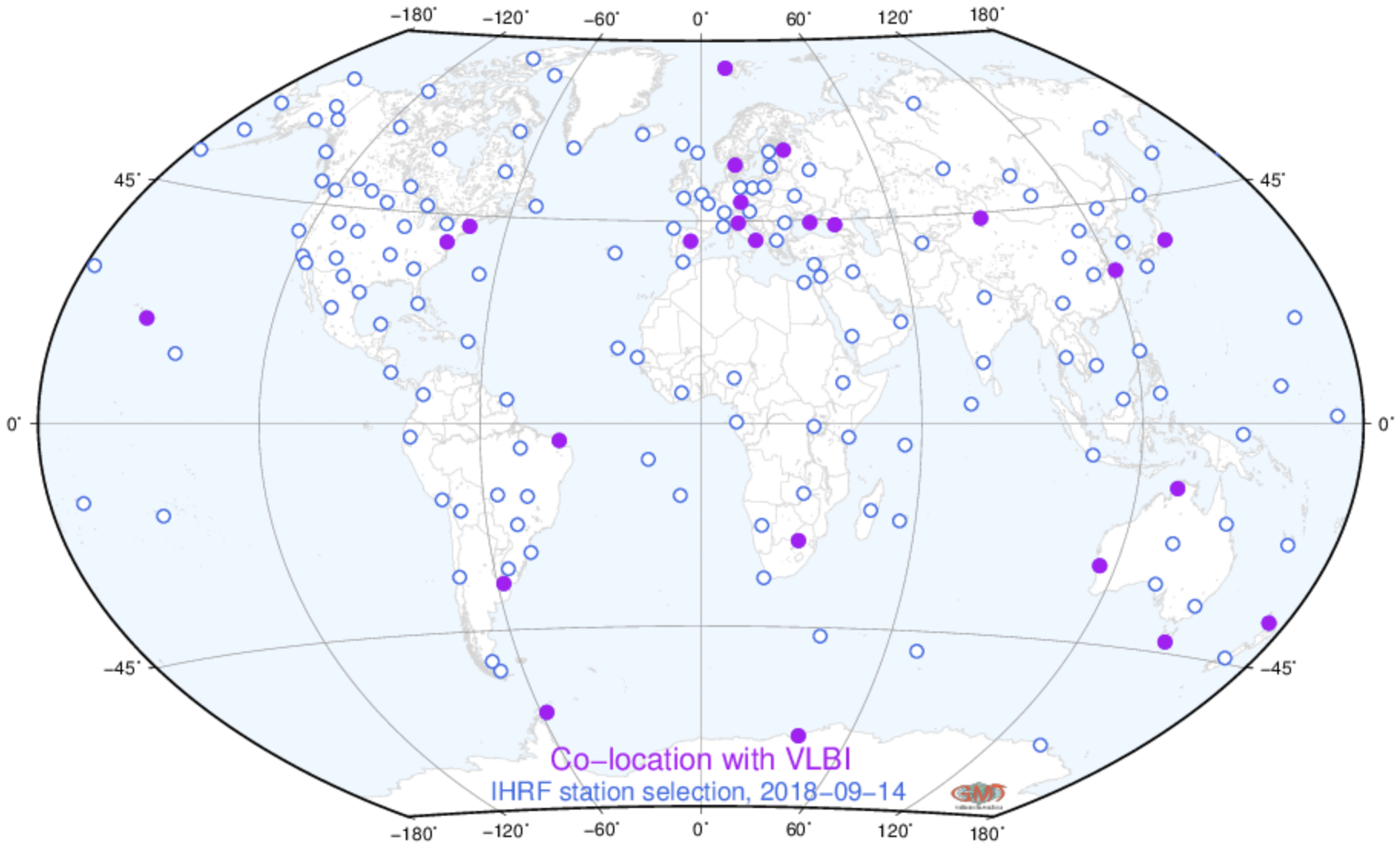
First proposal for the IHRF reference network: 165 selected sites



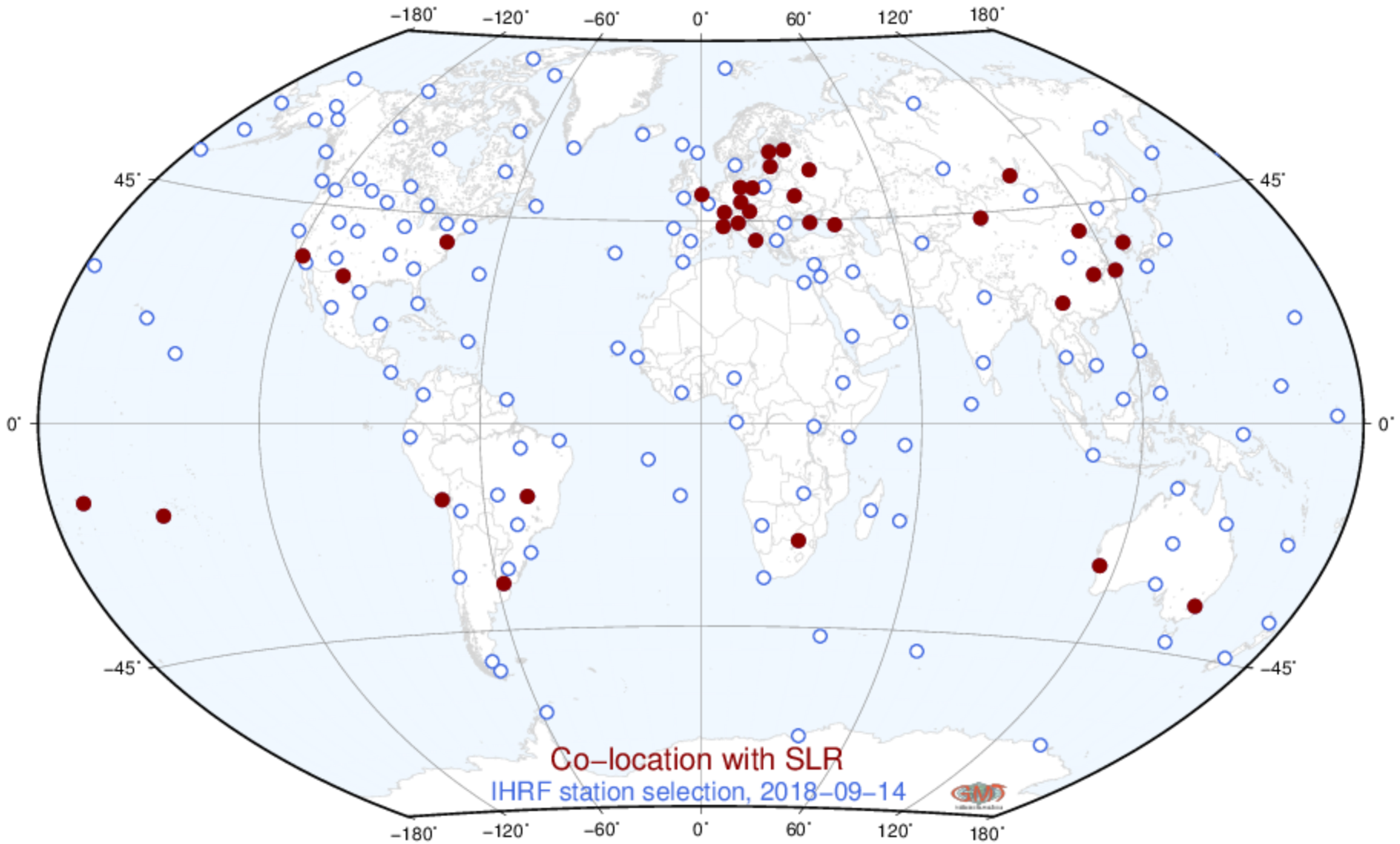
Interaction with regional/national experts for the IHRF station selection



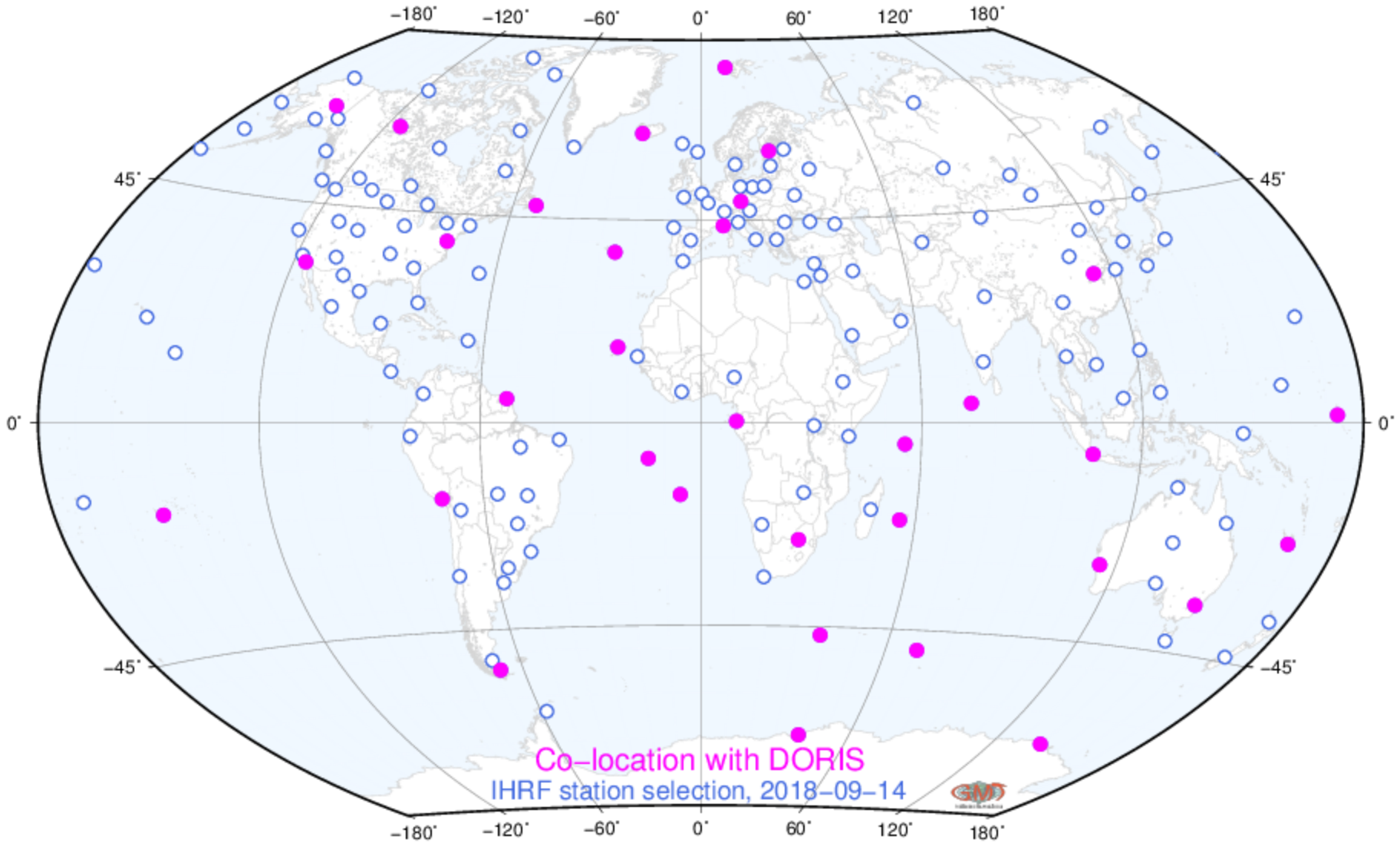
Co-location with VLBI (25 sites)



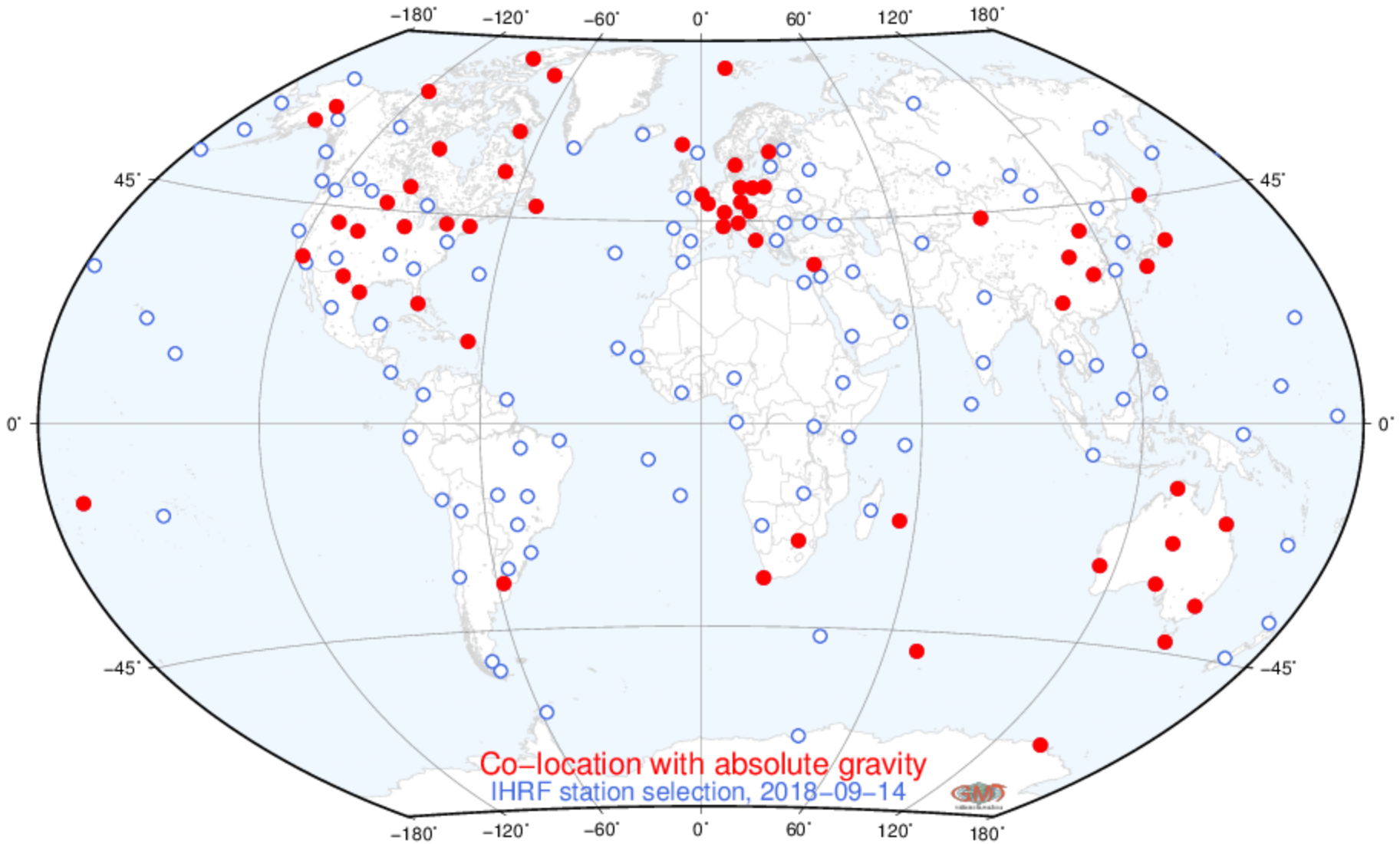
Co-location with SLR (35 sites)



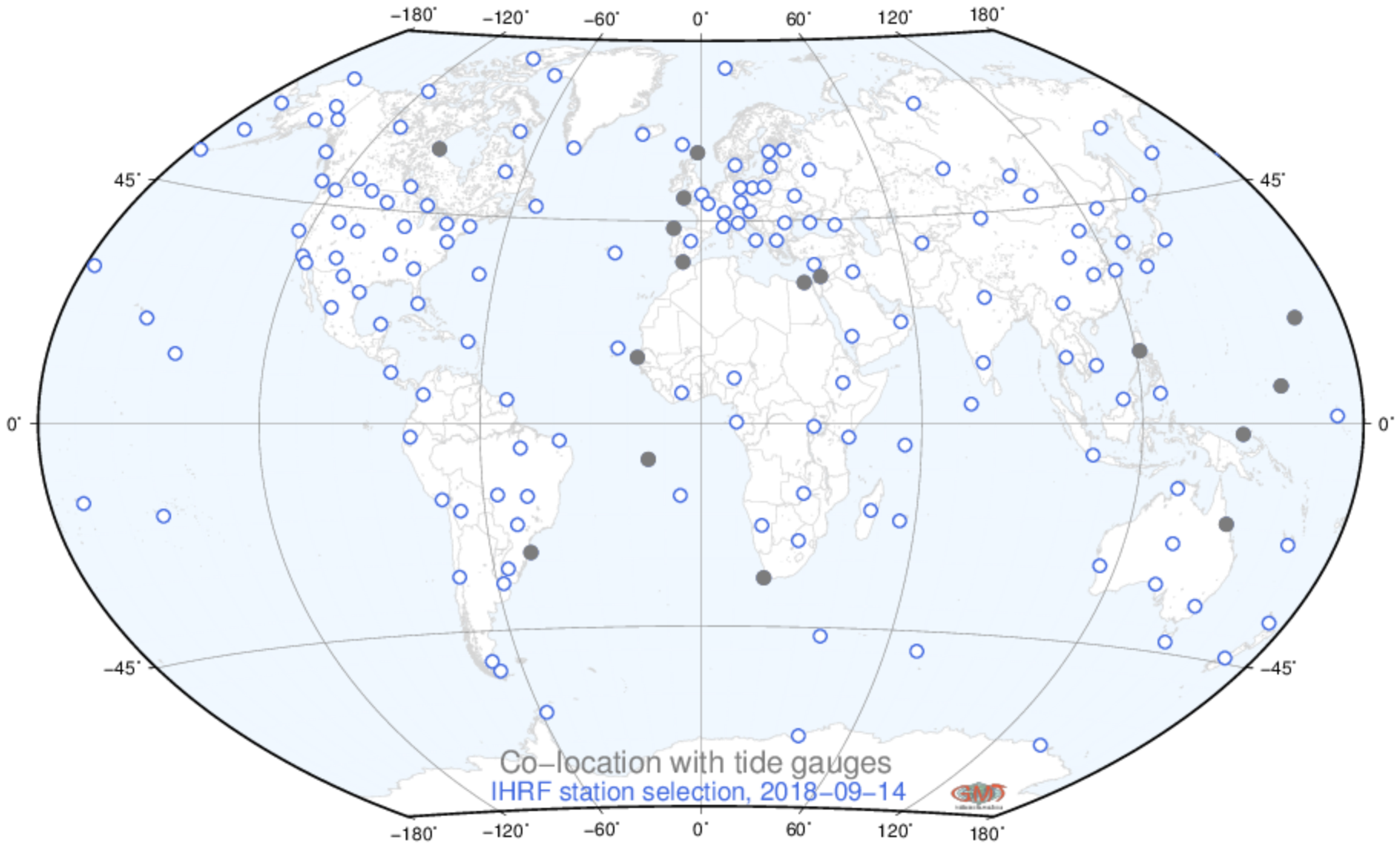
Co-location with DORIS (34 sites)



Co-location with absolute gravity (59 sites)



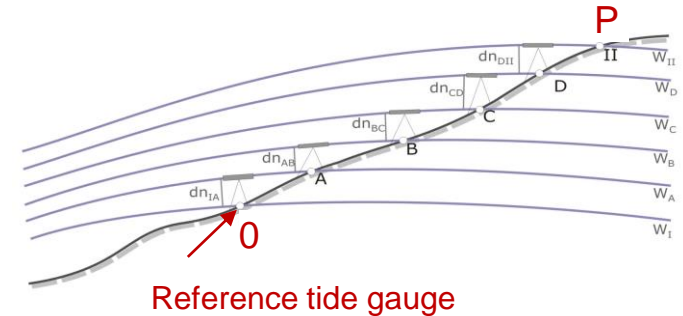
Co-location with tide gauges (15 sites)



Gravity-related vertical coordinates

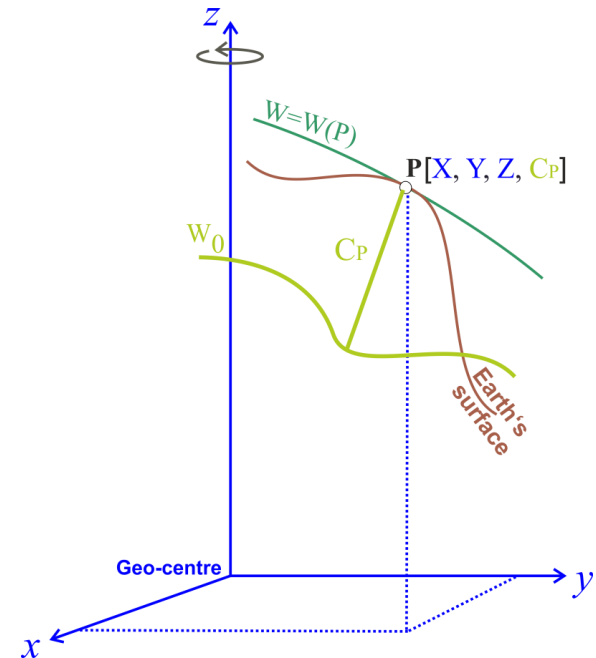
- In levelling, we determine **geopotential numbers** with respect to a reference tide gauge (**local vertical datum**)

$$H_P^{local} = \frac{W_0^{local} - W_P}{\hat{g}} = \frac{C_P^{local}}{\hat{g}} \quad ; \quad C_P = \cong \sum_0^P g \, dn$$



- Within the IHRS, we aim at determining **(global) geopotential numbers** with respect to a **global conventional reference potential** W_0 . As W_0 is a convention, known and fixed, the primary vertical coordinates are **potential values** W_P directly:

$$-\Delta W_P = C_P = W_0 - W_P$$



Computation of potential values $W(P)$

- 1) Global gravity models of high-degree (with RTM)

$$W_P = f(X_P, GGM)$$

- 2) High-resolution gravity field modelling:

$$W_P = W_{P, \text{satellite-only}} + W_{P, \text{high-resolution}}$$

Satellite-only gravity field modelling:
Satellite orbits and gradiometry analysis
Satellite tracking from ground stations (SLR)
Satellite-to-satellite tracking (CHAMP, GRACE)
Satellite gravity gradiometry (GOCE)
Satellite altimetry (oceans only)



High-resolution gravity field modelling:
Stokes or Molodenskii approach
Satellite altimetry (oceans only)
Gravimetry, astro-geodetic methods, levelling, etc.
Terrain effects

- 3) Potential values recovered from existing (quasi)-geoid models:

$$W_P = U_P + \gamma \zeta_P + (W_0 - U_0)$$

- 4) Levelling + gravimetry (after vertical datum unification):

$$W_P = (W_0^{local} + \delta W) - C_P; \quad \delta W = W_0^{IHRF} - W_0^{local}$$

Activities related to the IHRF coordinates (1/2)

1) **Sep. 2016 to Mar. 2017:** Strategy for the integration (transformation) of existing vertical datums into the IHRF/IHRF

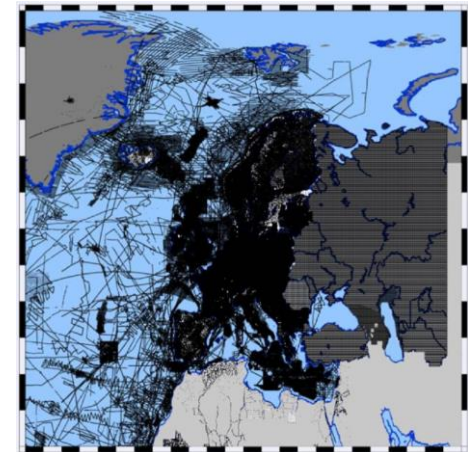
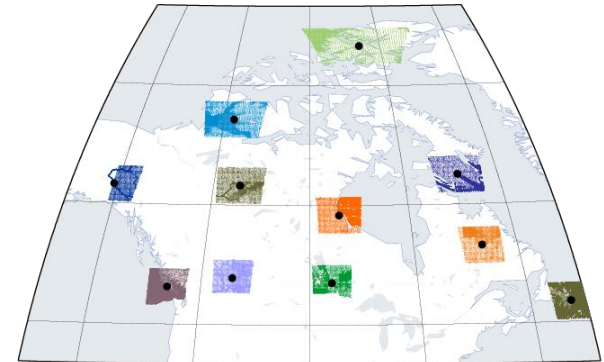
2) **May to Aug. 2017:**

a) Computation of potential values using the latest **GGMs of high-resolution:**

- EGM2008 (Pavlis et al., 2012), $l_{max} = 2190$
- EIGEN-6C4 (Förste et al., 2014), $l_{max} = 2190$
- XGM2016 (Pail et al., 2017), $l_{max} = 719$, extended to $l_{max} = 2190$ with EIGEN-6C4

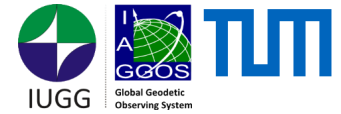
b) Comparison with potential values inferred from high-resolution gravity field modelling in Canada (NRCan, [M. Véronneau](#), [J. Huang](#)) and Europe (IFE/LUH, Germany [H. Denker](#))

c) Further numerical experiments in Greece (AUTH, [G. Vergos](#)), Brazil (EPUSP, [D. Blitzkow](#), [A.C.O.C. Matos](#)) and Ecuador (UFPR, [S. Freitas](#) and [J.L. Carrión-Sánchez](#))



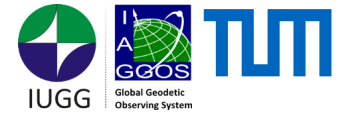
After Denker (2015)

Conclusions from the activities in 2017



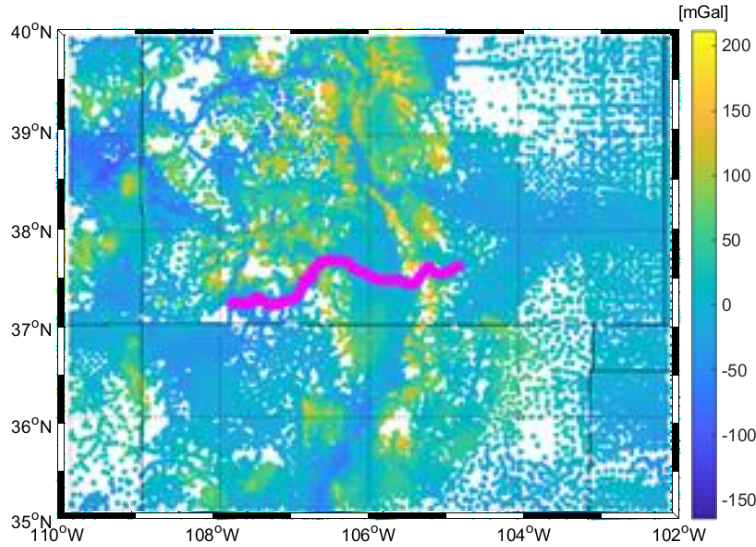
- 1) The use of **GGMs is (at present) not suitable** for the estimation of precise potential values. GGMs may be used if „**no other way**“.
- 2) Results obtained from high-resolution gravity field modelling present **discrepancies up to the dm-level**.
- 3) A “**standard**” procedure for the computation of potential values may be not appropriate as
 - different data availability and different data quality exist around the world
 - regions with different characteristics require particular approaches (e.g. modification of kernel functions, size of integration caps, geophysical reductions like GIA, etc.)
- 4) A “**centralized**” computation (like in the ITRF) is complicated due to the restricted accessibility to terrestrial gravity data
- 5) **What should we do?** - Discussions at the IAG-IASPEI Assembly (Aug. 2017):
 - To compute IHRF coordinates using **exactly the same input data** and the **own methodologies (software)** of colleagues involved in the gravity field modelling
 - Based on the comparison of the results, to identify a **set of standards** that allow to get **as similar and compatible results as possible**.

Activities related to the IHRF coordinates (2/2)

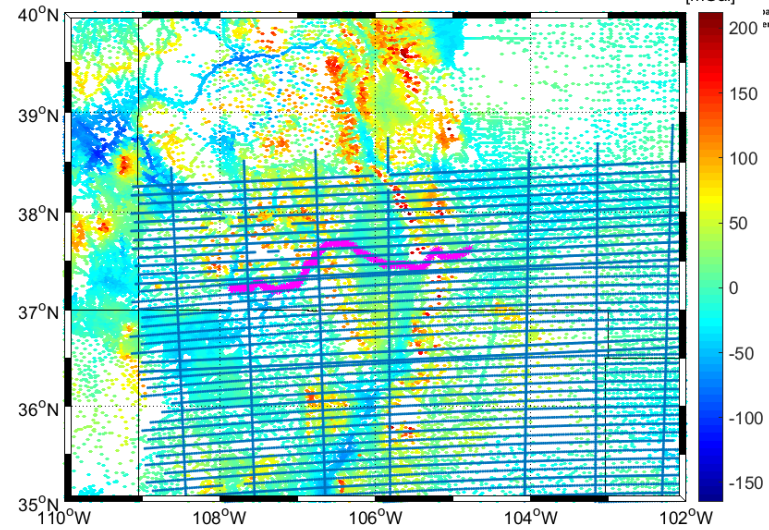


- 1) **Aug. 2017**: YM Wang (NGS/NOAA), chair of the IAG JWG 2.2.2 ([The 1 cm geoid experiment](#)) proposes the distribution of gravity data, terrain model and GNSS/levelling data for an area of about 500 km x 800 km in Colorado, USA → [Colorado experiment](#)
- 2) Participants in the Colorado experiment should compute [geoid](#), [quasi-geoid](#), and [potential values](#) at selected points
- 3) This experiment is performed within:
 - GGOS JWG: [Strategy for the realisation of the IHRS](#) (chair: L. Sánchez)
 - IAG JWG 2.2.2: [The 1 cm geoid experiment](#) (chair: Y.M. Wang)
 - IAG SC 2.2: [Methodology for geoid and physical height systems](#) (chair: J. Ågren)
 - ICCT JSG 0.15: [Regional geoid/quasi-geoid modelling - Theoretical framework for the sub-centimetre accuracy](#) (chair: J. Huang)
- 4) **Dec. 2017 - Jan. 2018**: A set of basic (minimum) standards/requirements for the computation of potential values was prepared
- 5) **Feb. 2018**: The Colorado data was distributed
- 6) **Since Feb. 2018**: Different computation groups are working with these data.

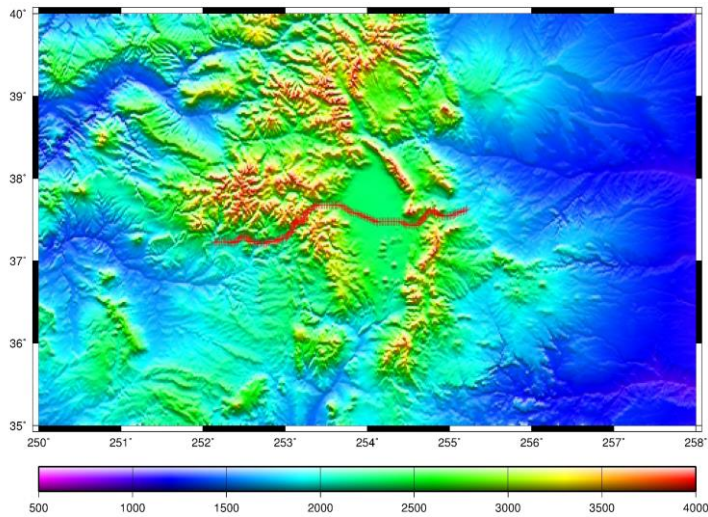
Colorado data



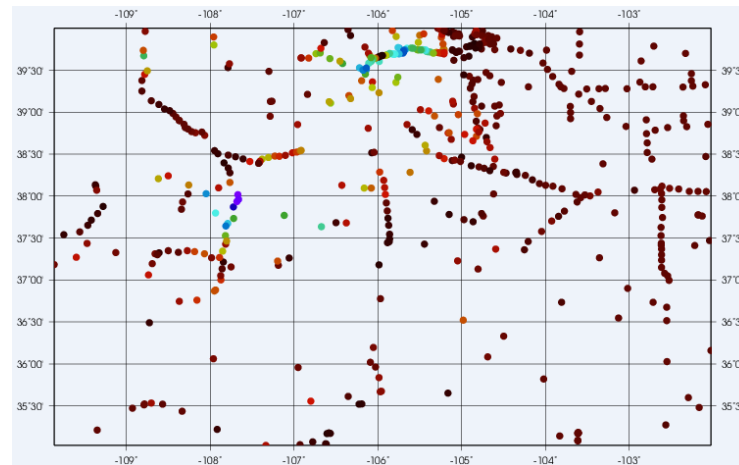
Surface gravity data (59,303 points)



Airborne gravity data
(41 lines E-W, 7 lines N-S)



Terrain model: SMRT V4.1



NGS *historical* GPS/levelling (510 points)

Contributing solutions



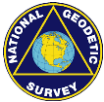
Faculty of Engineering, Minia University, Egypt → N



Istanbul Teknik Üniversitesi, Istanbul, Turkey → N ζ



Department of Geodesy and Surveying, Aristotle University of Thessaloniki, Thessaloniki, Greece → N ζ W



National Geodetic Survey, USA → N ζ W



Natural Resources Canada, Canada → N ζ W

LANTMÄTERIET

Lantmäteriet, Swedish mapping, cadastral and land registration authority, Sweden → N ζ W



School of Earth and Planetary Sciences and The Institute for Geoscience Research, Curtin University, Australia → N ζ W



Universidade Federal do Parana, Brazil → N ζ W



Escola Politécnica, Universidade de São Paulo; Centro de Estudos de Geodesia, Brazil → T



Deutsches Geodätisches Forschungsinstitut, Technische Universität München, Germany → W

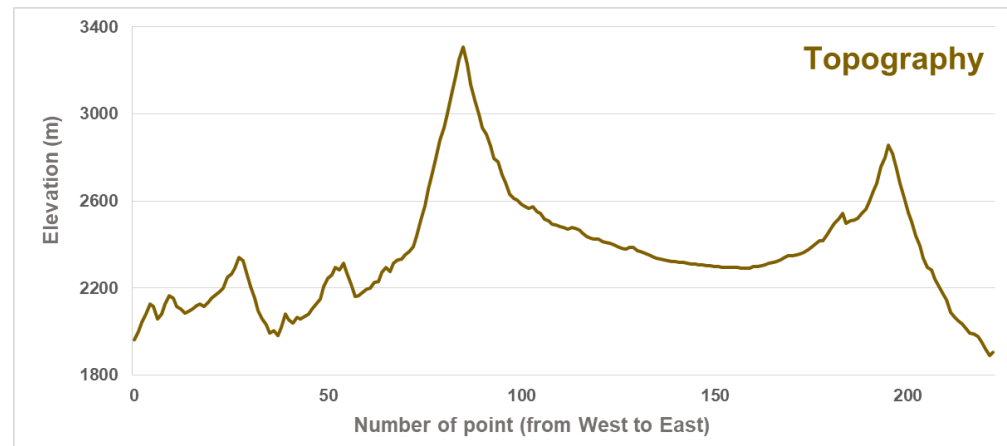
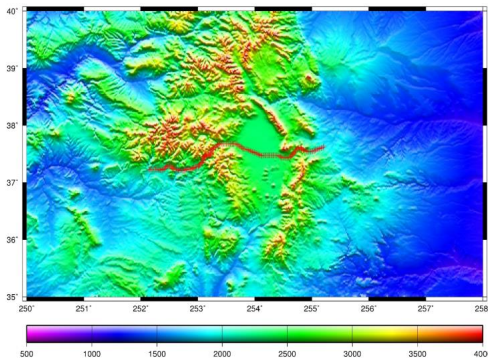
Comparison of potential values $W(P)$ (1/4)

- 1) The comparison is carried out at 223 GSVS17 marks (Geoid Slope Validation Survey 2017) selected by NGS
- 2) Participants in the experiment got φ , λ , h ; levelling is not available (yet).
- 3) The potential values provided by the different solutions are converted to geopotential numbers with respect to the ITRS W_0 value

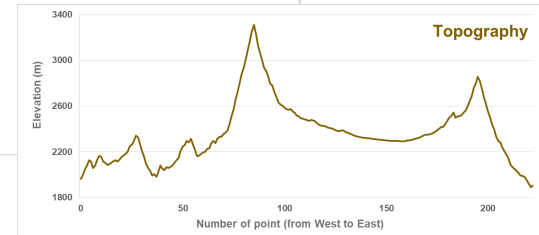
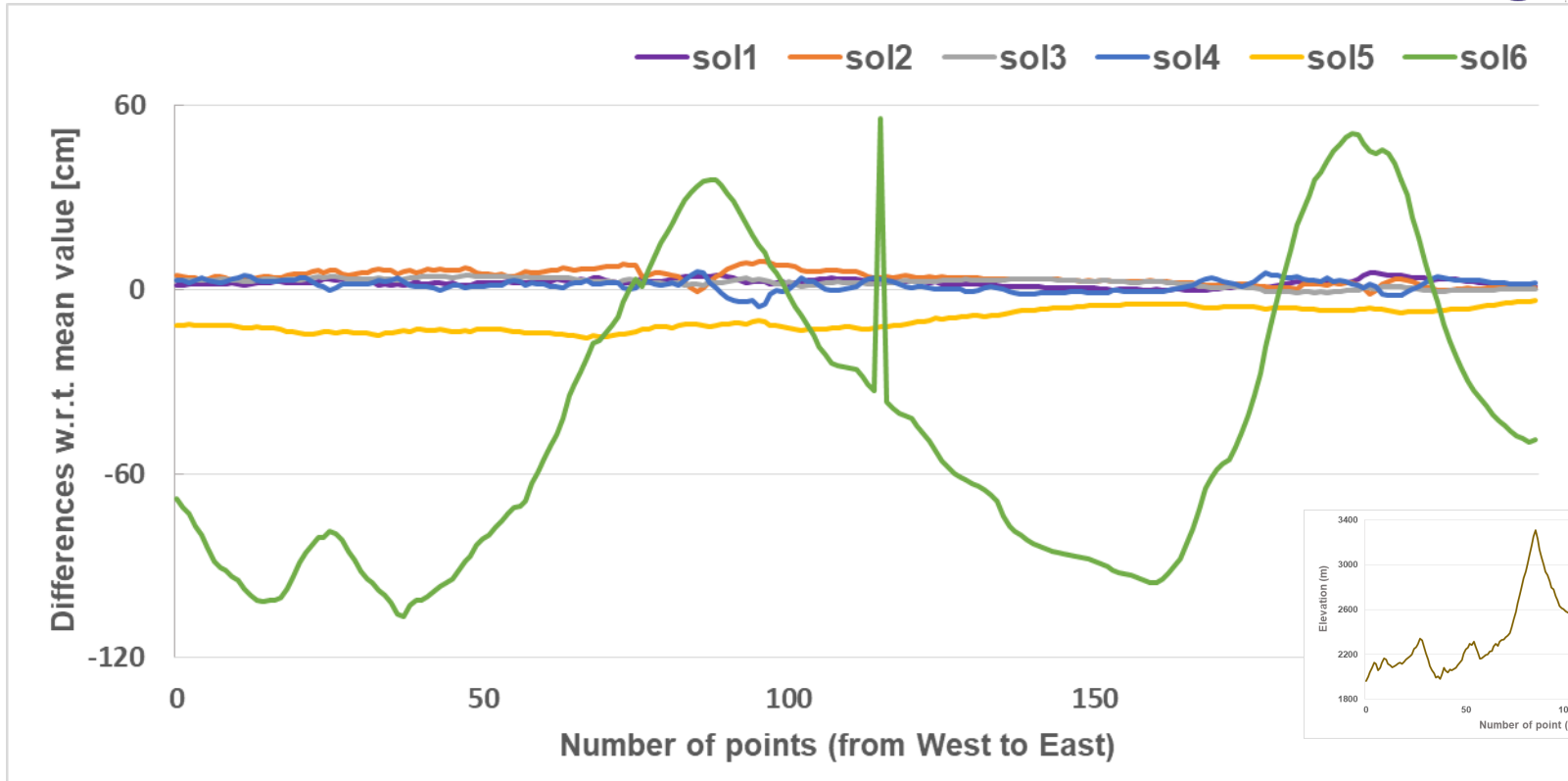
$$C(P) = W_0 - W(P) \quad ; \quad W_0 = 62\,636\,853.4 \text{ m}^2\text{s}^{-2}$$

- 2) and further transformed to normal heights (to see the differences in meters):

$$H^*(P) = C(P)/\gamma(P)$$



Comparison of potential values W(P) (2/4)



sol1: $\zeta \rightarrow W$

sol2: $N \rightarrow W$

sol3: W

sol4: $N \rightarrow W$

sol5: $\zeta \rightarrow W$

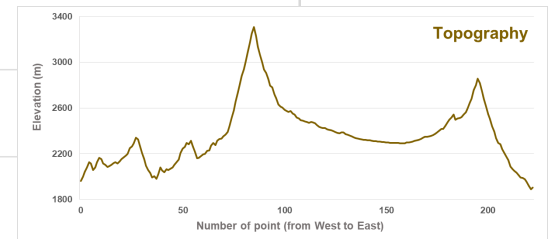
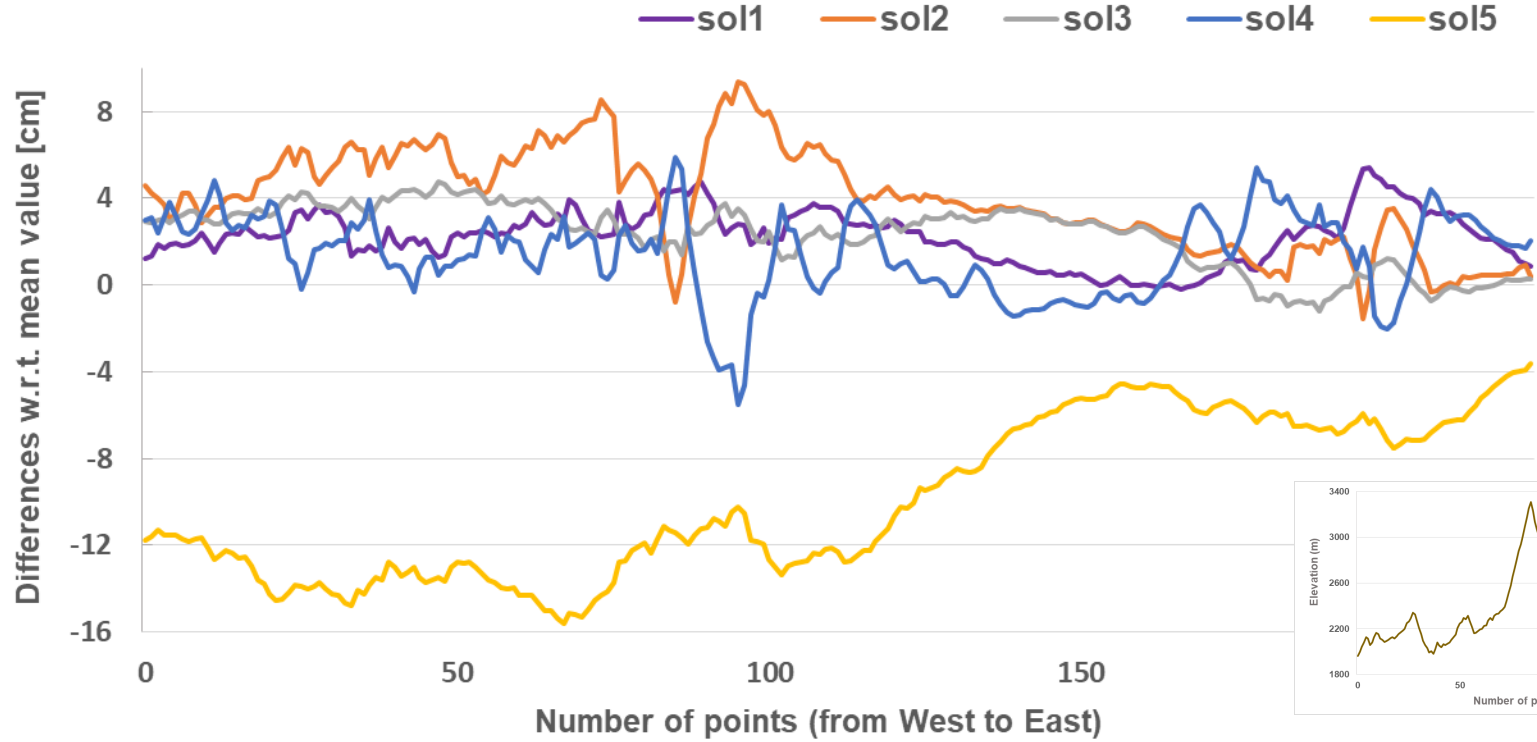
sol6: $\zeta \rightarrow W$

	sol1	sol2	sol3	sol4	sol5	sol6
mean [cm]	2.2	3.9	2.3	1.4	-9.9	-42.9
std [cm]	1.2	2.3	1.5	1.9	3.6	47.0
max [cm]	5.4	9.4	4.8	5.9	-3.6	55.8
min [cm]	-0.2	-1.6	-1.2	-5.5	-15.6	-106.6
range [cm]	5.6	11.0	6.0	11.4	19.2	162.4

Comparison of potential values W(P) (3/4)



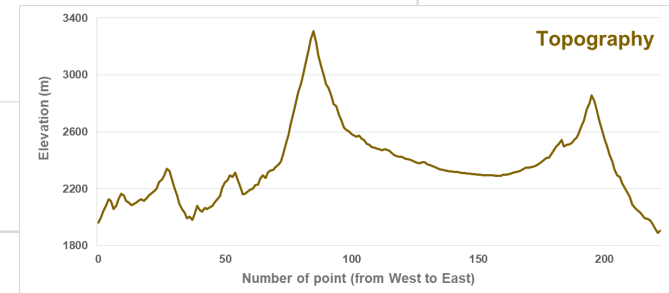
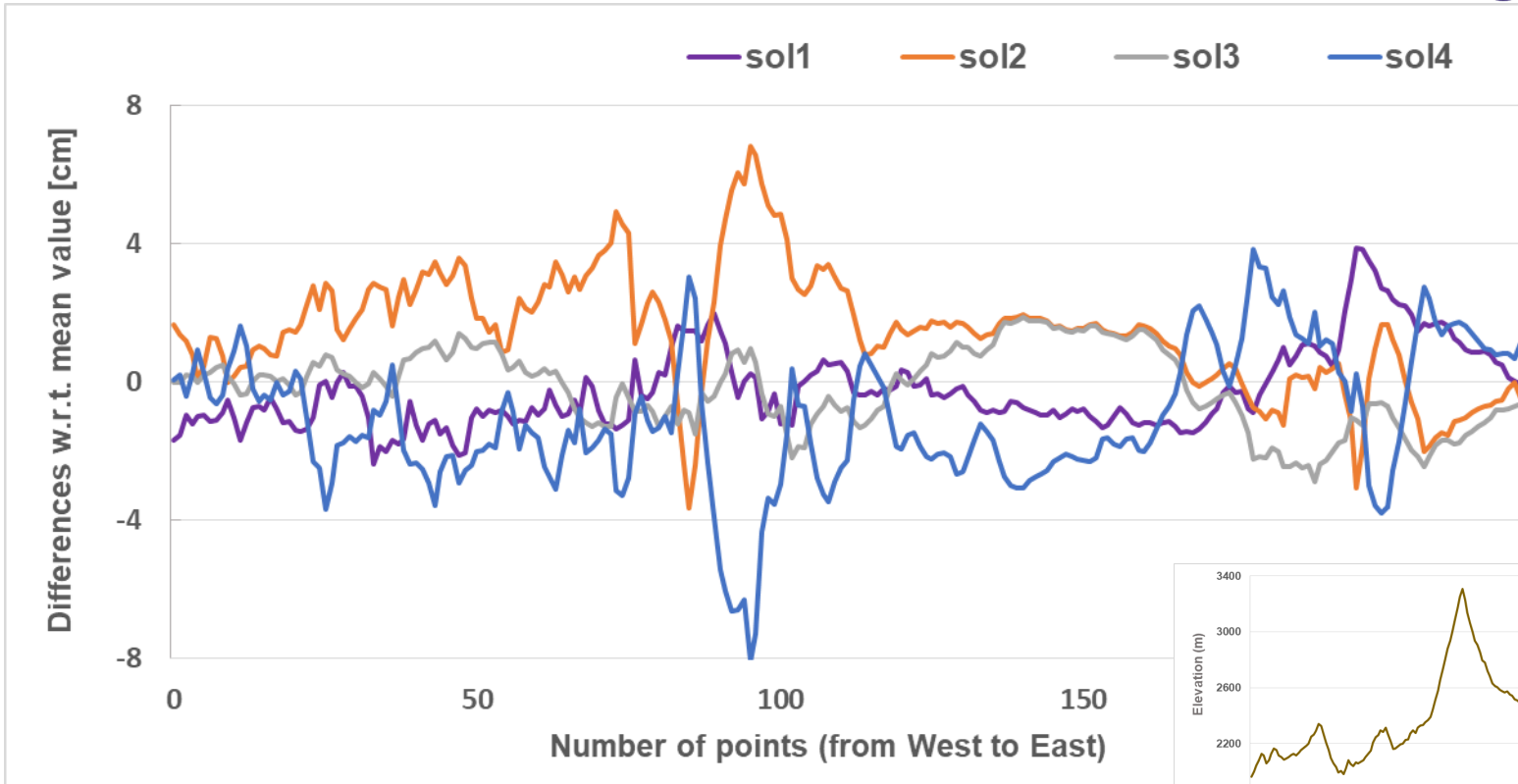
Global Geodetic Observing System



- sol1:** $\zeta \rightarrow W$
- sol2:** $N \rightarrow W$
- sol3:** W
- sol4:** $N \rightarrow W$
- sol5:** $\zeta \rightarrow W$

	sol1	sol2	sol3	sol4	sol5
mean [cm]	2.2	3.9	2.3	1.4	-9.9
std [cm]	1.2	2.3	1.5	1.9	3.6
max [cm]	5.4	9.4	4.8	5.9	-3.6
min [cm]	-0.2	-1.6	-1.2	-5.5	-15.6
range [cm]	5.6	11.0	6.0	11.4	19.2

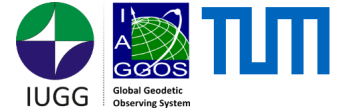
Comparison of potential values W(P) (4/4)



- sol1:** $\zeta \rightarrow W$
- sol2:** $N \rightarrow W$
- sol3:** W
- sol4:** $N \rightarrow W$

	sol1	sol2	sol3	sol4
mean [cm]	-0.2	1.5	-0.2	-1.1
std [cm]	1.2	1.7	1.1	2.0
max [cm]	3.9	6.8	1.9	3.8
min [cm]	-2.4	-3.6	-2.9	-8.1
range [cm]	6.3	10.5	4.7	11.9

Main conclusions from the Colorado experiment



- 1) Four (of seven) solutions are consistent in the **1 dm level**, with agreement within **1 cm to 2 cm** in terms of standard deviation with respect to the mean value
- 2) Discrepancies present a **strong correlation with the topography**
- 3) To be the first (preliminary) results, they are **very promising**
- 4) A **convergence** of the results at the **1 cm** level may be **reachable**

Next steps

- 1) To identify **sources of discrepancy** between the different solutions
- 2) To compute **refined solutions** (two or more iterations)
- 3) To compare **potential differences with geopotential values** derived from levelling and gravimetry (when NGS releases these data)
- 4) To compile a first version of **“the IHRS standards and conventions”**.

Outlook

- 1) The first version of “**the IHRF standards and conventions**” should be ready for discussion before the next IUGG General Assembly in Montreal, July, 2019
- 2) A **first (static) solution for the IHRF** will be presented at the IUGG General Assembly: it should be **preliminary** and it is to identify **drawbacks and required improvements**
- 3) For the next term 2019-2023, a joint working group of the GGOS FA-UHS, IAG Commission 2 and the IGFS should investigate the best way to establish an ‘**IHRF element**’ **within the IGFS** to ensure the maintenance and availability of the IHRF:
 - Regular updates of the **IHRF_{yyyy}** to take account for:
 - new stations;
 - coordinate changes with time $\dot{\mathbf{X}}, \dot{W}$;
 - improvements in the estimation of \mathbf{X} and W (more observations, better standards, better models, better computation algorithms, etc.)
 - Geodetic **products associated** to the IHRF (description and metadata).
 - Organizational and operational **infrastructure to ensure the IHRF sustainability**.

This work is possible thanks to the **contribution of many colleagues**. Their support is **deeply acknowledged**:

A. Álvarez, A.C.O.C. Matos, B. Erol, C. Brunini, C. Estrella, C. Iturriaga, C.C. Carneiro, D. Avalos, D. Blitzkow, D. Piñon, D. Roman, D. Smith, D. van Westrum, G. Vergos, H. Abd-Elmotaal, H. Denker, H. Drewes, H. Wziontek, I. Liepiņš, I. Oshchepkov, J. Ågren, J. Chire, J. Huang, J. Ihde, J. Krynski, J. Mäkinen, J.L. Carrión-Sánchez, K. Ahlgren, K. Matsuo, L. Sjöberg, M. Amos, M. Filmer, M. Pearlman, M. Sideris, M. Varga, M. Véronneau, M. Willberg, N. Suárez, R. Barzaghi, R. Dalazoana, R. Forsberg, R. Pail, R.T. Luz, S. Claessens, S.M.A. Costa, S.R.C. Freitas, U. Marti, V. Grigoriadis, V. Lieb, V.G. Ferreira, W. Featherstone, Y.M. Wang ...

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